

Integral Aufgabe 143

Berechnen Sie den Flächeninhalt A zwischen $f(x) = (1/3)x^2$ und $g(x) = x - (1/12)x^3$.

Schnittpunkte:

$$f(x) = g(x)$$

$$\frac{1}{3}x^2 = x - \frac{1}{12}x^3 \quad | \cdot 12$$

$$4x^2 = 12x - x^3 \quad | +x^3 - 12x$$

$$x^3 + 4x^2 - 12x = 0$$

$$x(x^2 + 4x - 12) = 0$$

$$x_1 = 0$$

$$x^2 + 4x - 12 = 0$$

Linearfaktoren:

$$x^2 + 4x - 12 = (x + 6)(x - 2)$$

$$x_2 = -6$$

$$x_3 = 2$$

$$f(x) - g(x) = \frac{1}{3}x^2 - (x - \frac{1}{12}x^3) = \frac{1}{3}x^2 - x + \frac{1}{12}x^3$$

$$A = \int_{-6}^0 (\frac{1}{3}x^2 - x + \frac{1}{12}x^3) dx + \int_0^2 (\frac{1}{3}x^2 - x + \frac{1}{12}x^3) dx$$

$$A = \left| \frac{x^3}{9} - \frac{x^2}{2} + \frac{x^4}{48} - \frac{0}{-6} \right| + \left| \frac{x^3}{9} - \frac{x^2}{2} + \frac{x^4}{48} - \frac{2}{0} \right|$$

$$A = |0 - (-24 - 18 + 27)| + |0,89 - 2 + 0,33 - 0|$$

$$A = |15| + |-0,78|$$

$$\mathbf{A = 15,78}$$

